

# Chaos-Assisted Tunneling in Atom Optics

Final Defense 10/5/01

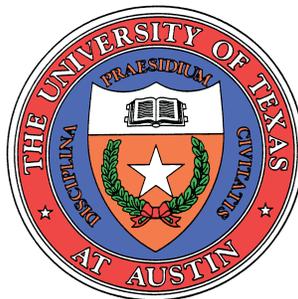
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Support:

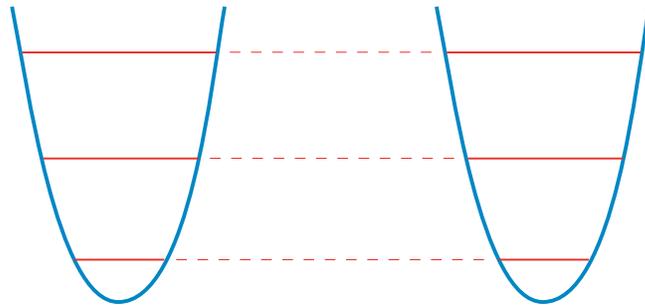
National Science Foundation

R. A. Welch Foundation

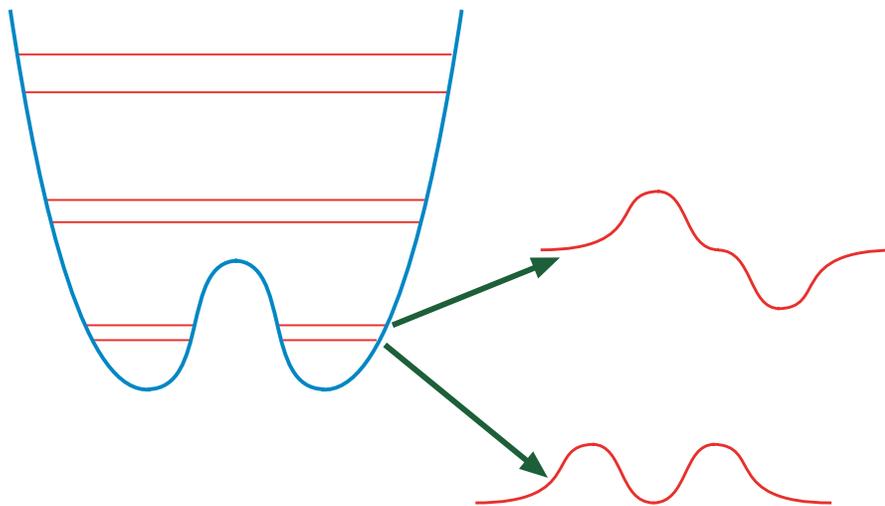
Fannie and John Hertz Foundation

# Barrier Tunneling

- Phase-space tunneling is related to tunneling in the double well potential
- Uncoupled limit: degenerate energy doublets



- Coupling (via the finite barrier) between the two wells leads to broken degeneracy and doublet structure

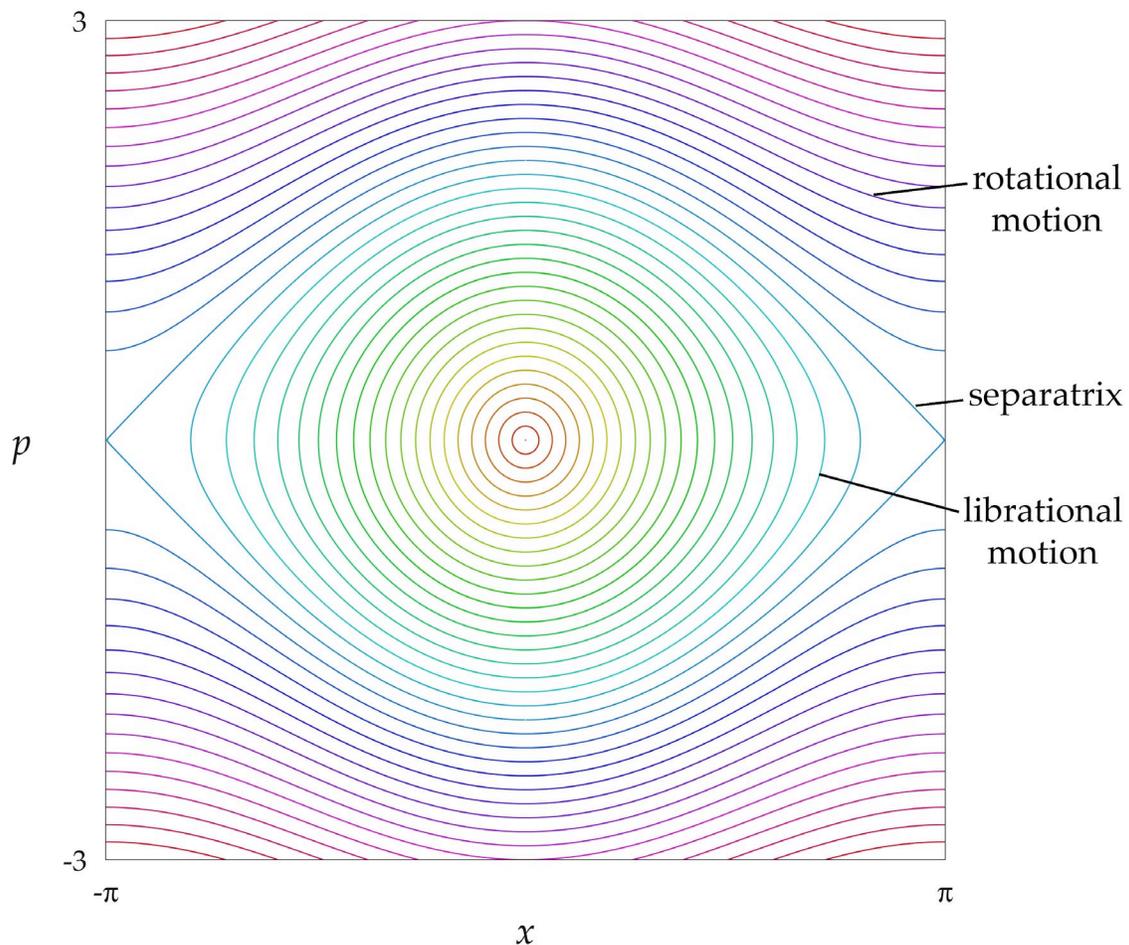
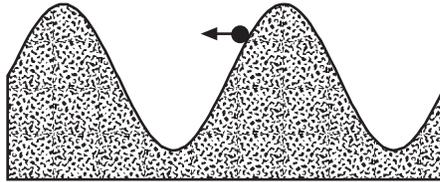


- Tunneling (Rabi oscillations) occur as the doublet states dephase
- Symmetry is important for tunneling, causes degeneracy in uncoupled limit (resonant Rabi oscillations)

# Phase Space

- Graphical representation of the equations of motion

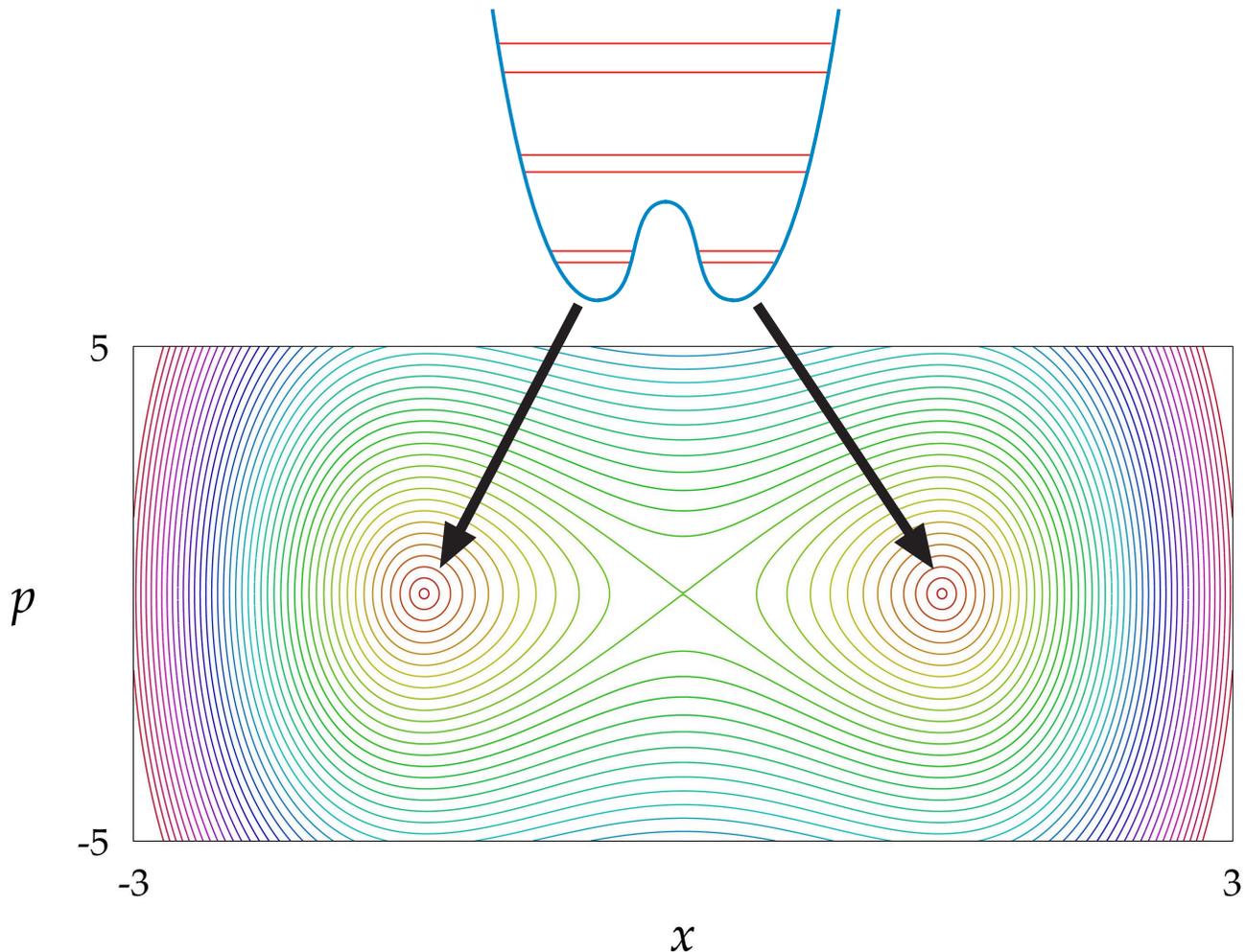
- Pendulum phase space:



- Integrable systems: trajectories confined to surfaces of lower dimension in phase space

# Double-Well Phase Space

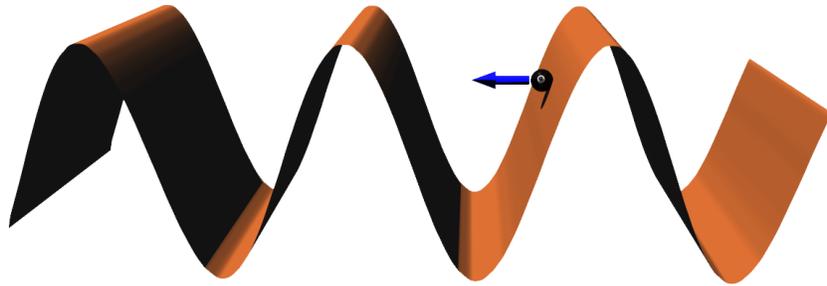
- Can think of barrier tunneling in phase space



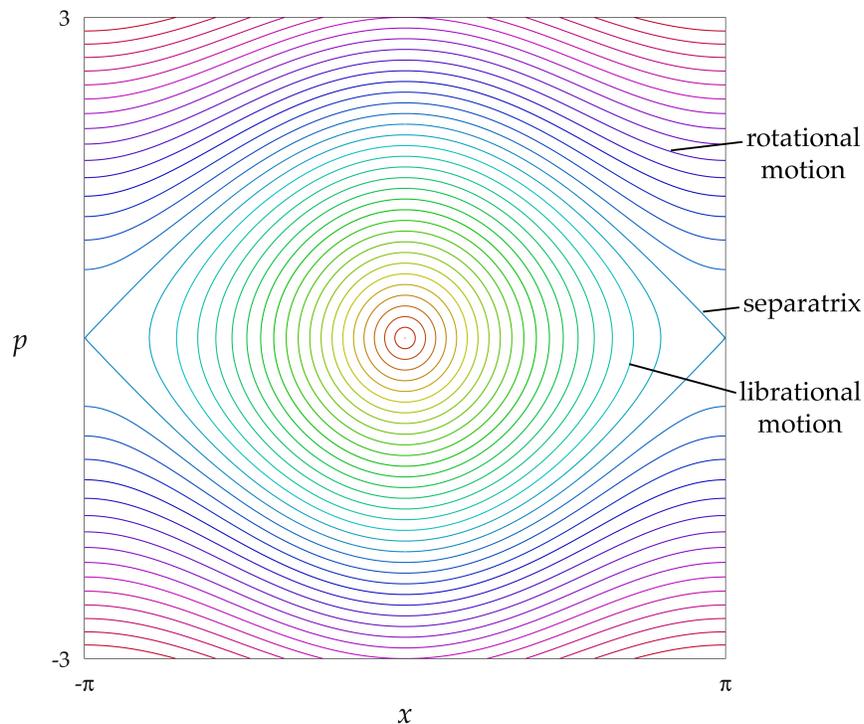
- Classical transport is forbidden: trajectories cannot cross invariant surfaces
- Quantum transport allowed: quantum paths can cross invariant surfaces, but are exponentially suppressed
  - Leads to universal scaling:  $\omega \sim \exp(-1/\hbar)$

# Optical Lattices and Atom Optics

- Formed by retroreflecting a laser beam -- standing wave
  - stationary, 1-D sinusoidal intensity pattern:



- Far-detuned regime:
  - spontaneous (random) scattering negligible
  - intensity pattern creates **spatial potential**
- Atomic motion equivalent to pendulum:



# Amplitude Modulation

- Full amplitude modulation of standing wave intensity:

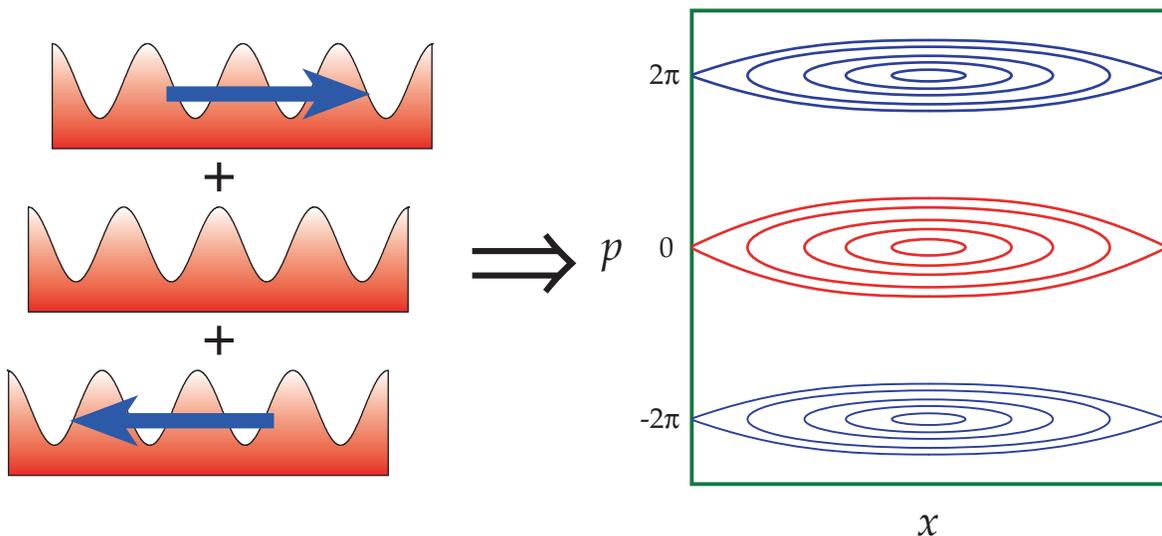
$$H = \frac{p^2}{2} - 2\alpha \cos^2(\pi t) \cos(x)$$

- Can rewrite potential as sum of 3 terms:

$$-\alpha \cos(x) - \frac{\alpha}{2} \cos(x + 2\pi t) - \frac{\alpha}{2} \cos(x - 2\pi t)$$

- one stationary and two moving lattices (pendula)

- Phase space contains three pendulum-like features:

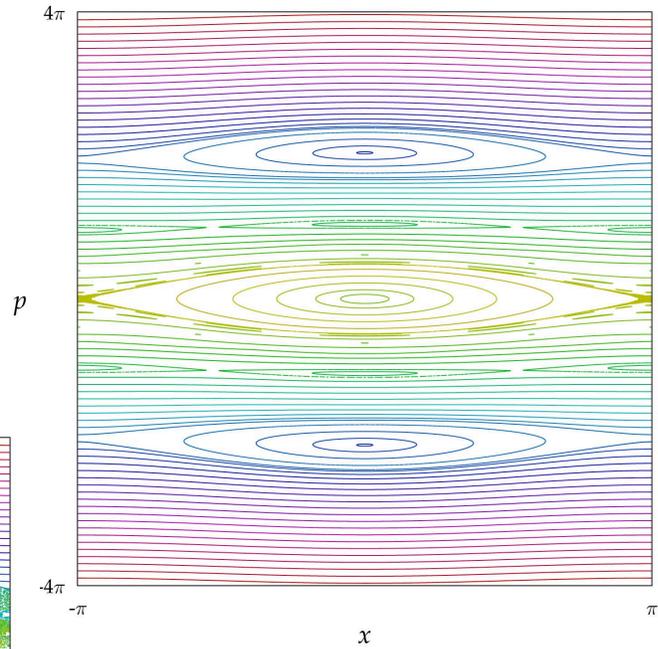


- Want to look for tunneling between two *symmetry-related* structures

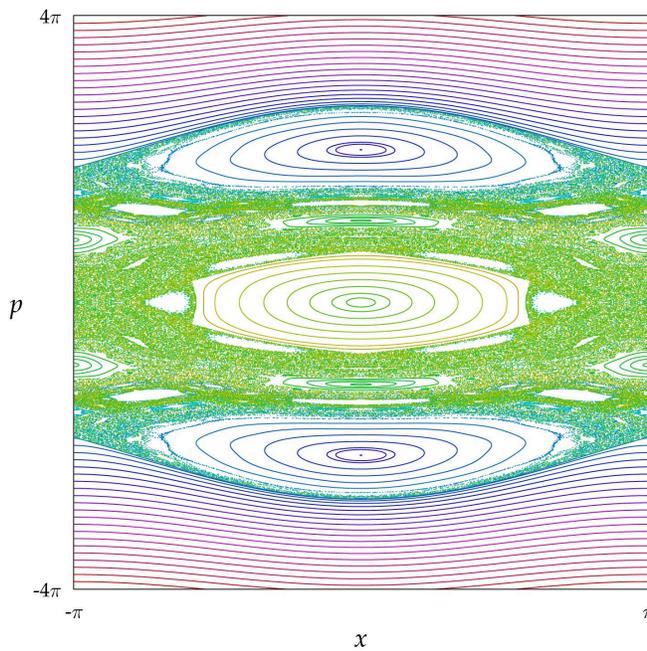
# Chaos in Phase Space

- As  $\alpha$  (well depth) increases, competition between the three modes of motion leads to chaos:

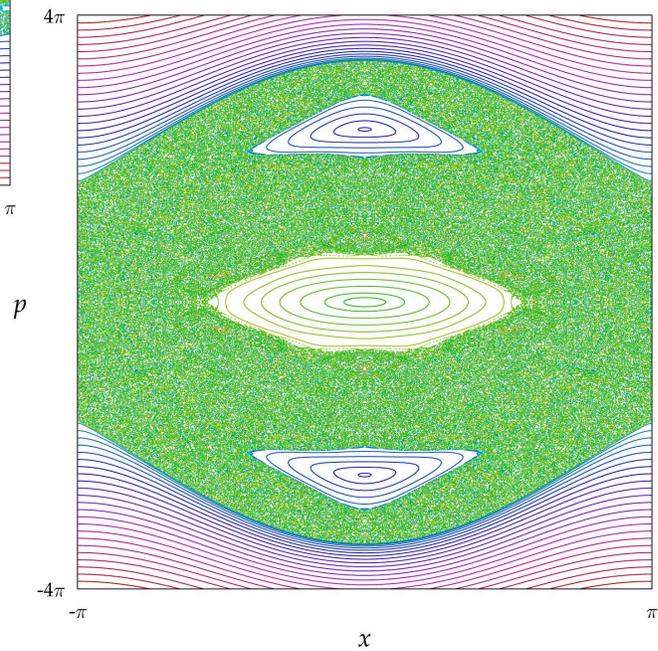
$$\alpha = 0.6$$



$$\alpha = 2.0$$

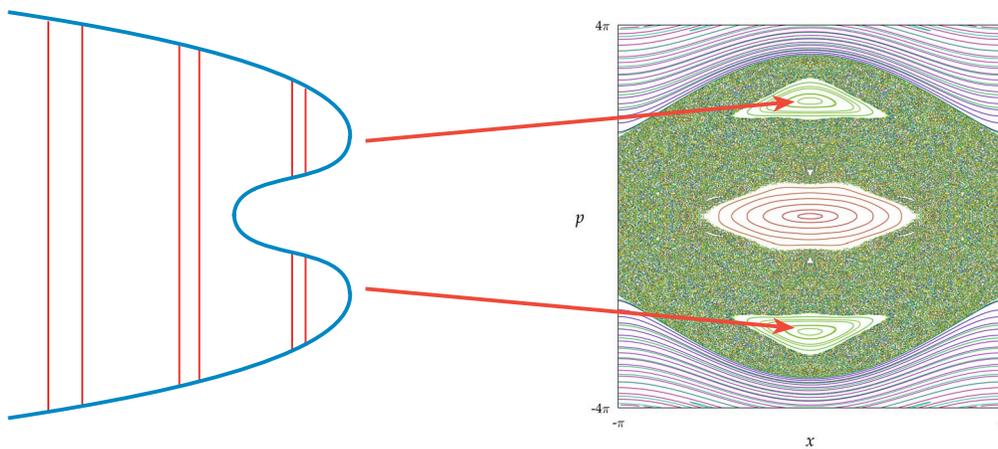


$$\alpha = 6.0$$



# Dynamical Tunneling

- In our system, islands play the role of the two wells
  - Islands case localization of Floquet states
  - Transport out of islands is classically forbidden

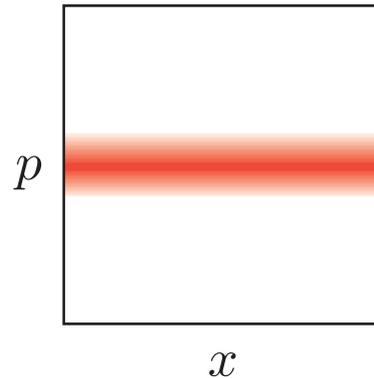


- Simplest picture: tunneling between symmetric islands proceeds as symmetric/antisymmetric Floquet-state pair dephase
- This tunneling is *dynamical tunneling*: transport is forbidden by the dynamics, not a potential barrier
- Predicted by Davis and Heller, 1981
- Also under study by NIST/U. Queensland collaboration

# “Simple” Experiment

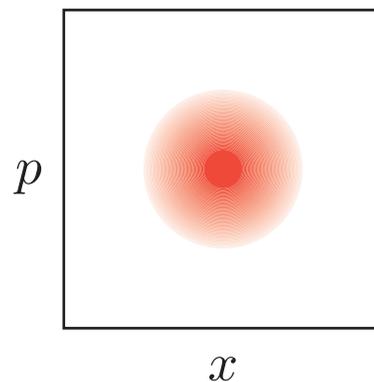
or “how not to observe tunneling”

- Simplified approach: cool cesium atoms in a 3-D optical lattice to 400 nK ( $\Delta p = 1.4\hbar k_L$ )

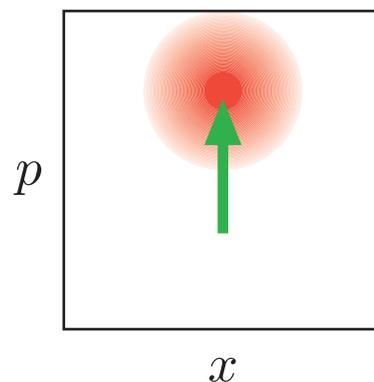


- Adiabatically turn on 1-D standing wave

- size is three times that of a minimum-uncertainty packet



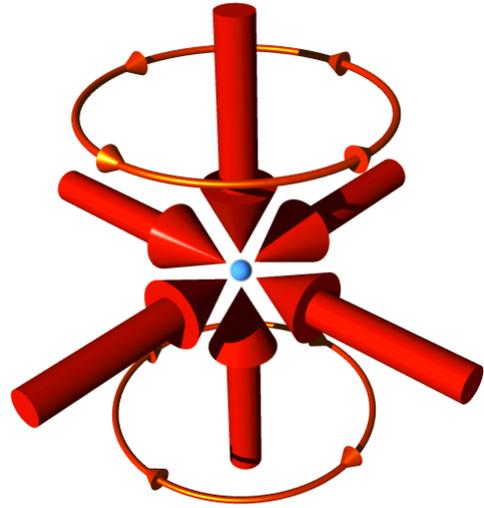
- Boost wave packet to match island velocity



- Modulate lattice to realize amplitude modulated pendulum...

# Measurement Sequence

1. Magneto-optic trap/  
preparation (5 s)



2. (State Preparation)  
(1 ms)

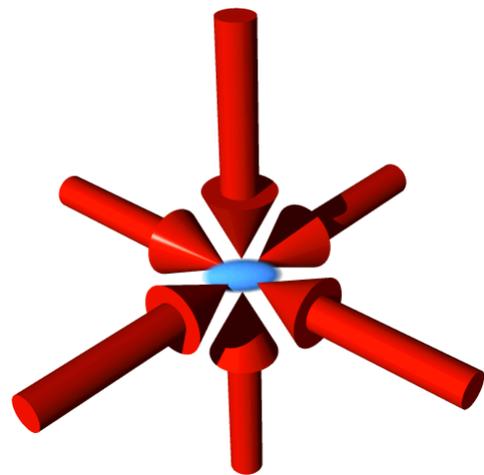
3. Time-Dependent  
Optical Lattice  
(1 ms)



4. Free expansion  
(15 ms)



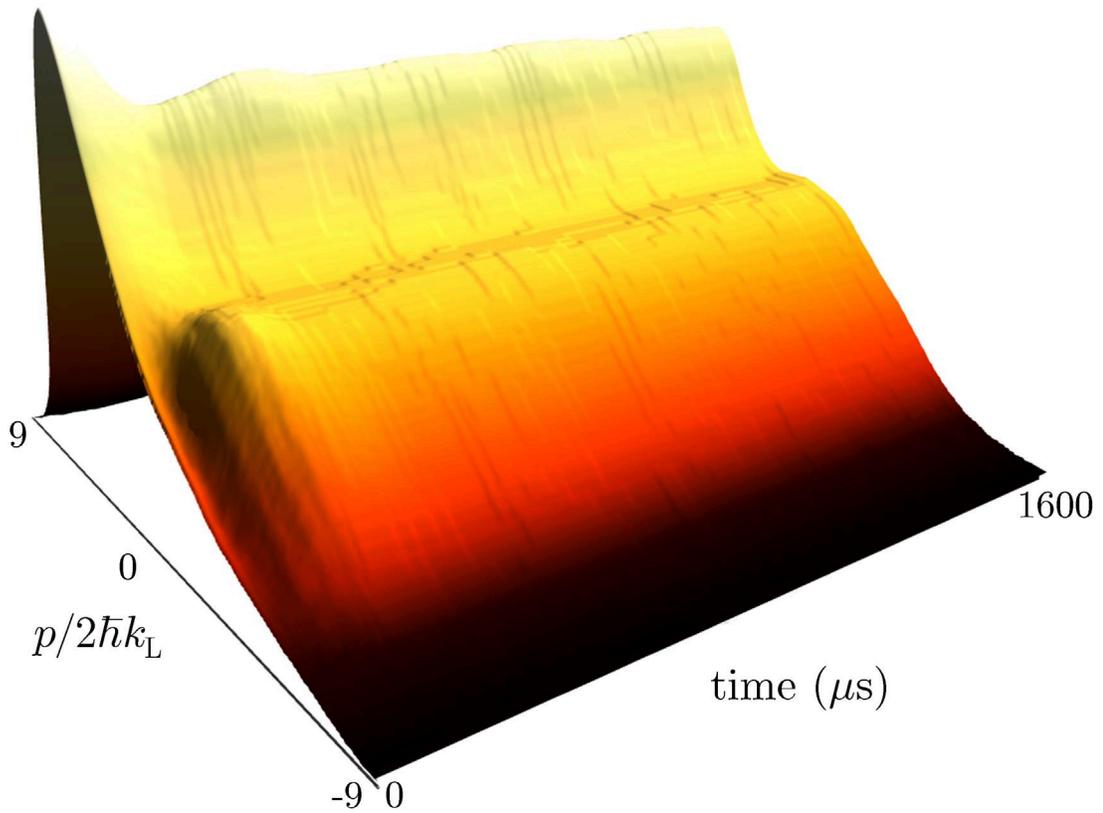
5. Freezing optical molasses/  
imaging (1 ms)



- Technique for measuring momentum distributions/energies

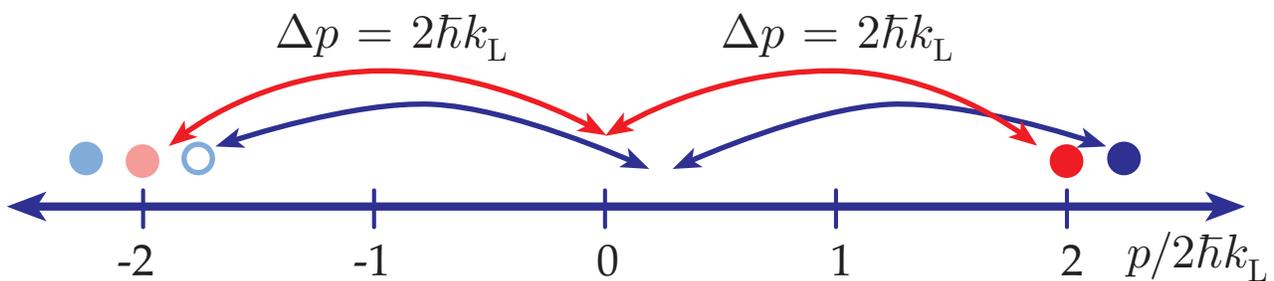
# Tunneling in Phase Space?

- Experimental momentum distributions vs. time:



# Symmetries

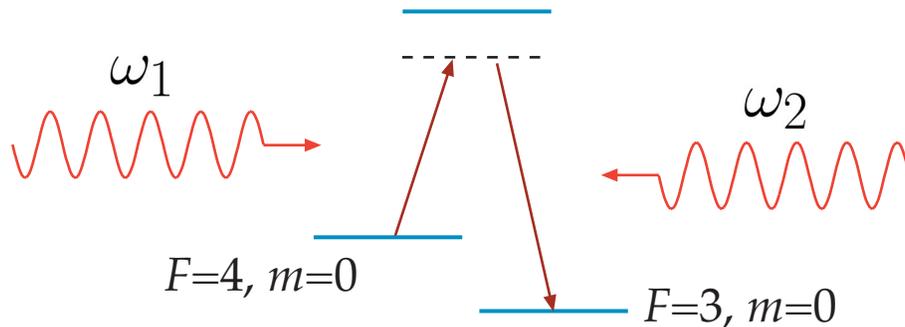
- *Classical symmetry*: satisfied due to island structure in phase-space
- *Quantum symmetry*: quantum mechanics imposes an additional symmetry
  - atoms change momentum in multiples of  $2\hbar k_L$
  - tunneling requires that states are coupled to their reflections about  $p = 0$  via these discrete steps



- Consequence: only certain “integer states” can tunnel
- Analogous to asymmetric double well or broken time-reversal symmetry
- Requires subrecoil velocity selection

# Raman Velocity Selection

- Use stimulated, two-photon transition between cesium ground states:



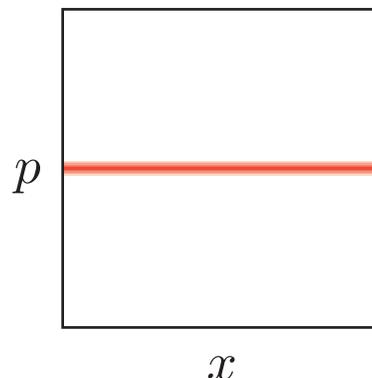
- If the two beams are counterpropagating, the atomic momentum enters into the resonance condition:

$$\omega_1 - \omega_2 = 2\pi \cdot 9.2 \text{ GHz} + \frac{p}{\hbar k_L} \cdot 4\omega_r$$

- Velocity selection procedure:

1. Optically pump to  $F = 4, m = 0$
2. Tag atoms with proper velocity into  $F = 3$
3. Push away  $F = 4$  atoms with resonant light

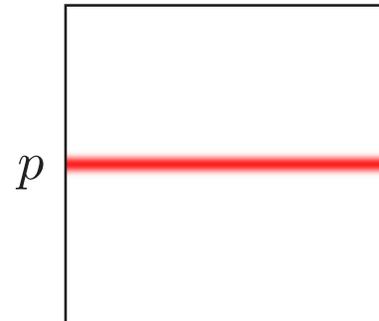
- Result: subrecoil atoms near  $p = 0$



# State Preparation

- Create localized state while preserving subrecoil structure

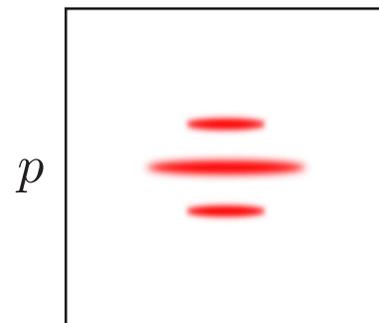
1. Begin with subrecoil sample from Raman tagging



2. Turn on 1-D standing wave adiabatically

- atoms become localized in the lattice wells, also heating

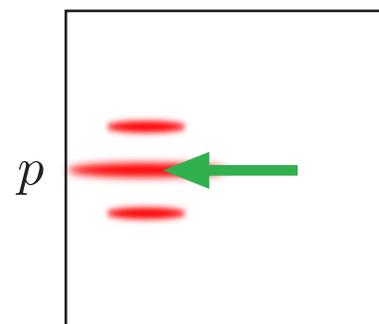
- subrecoil slices within overall profile  $\Rightarrow$  coherence over several wells



- minimum uncertainty for deep wells

3. Sudden shift of standing-wave phase

- using phase modulator before standing-wave retroreflector



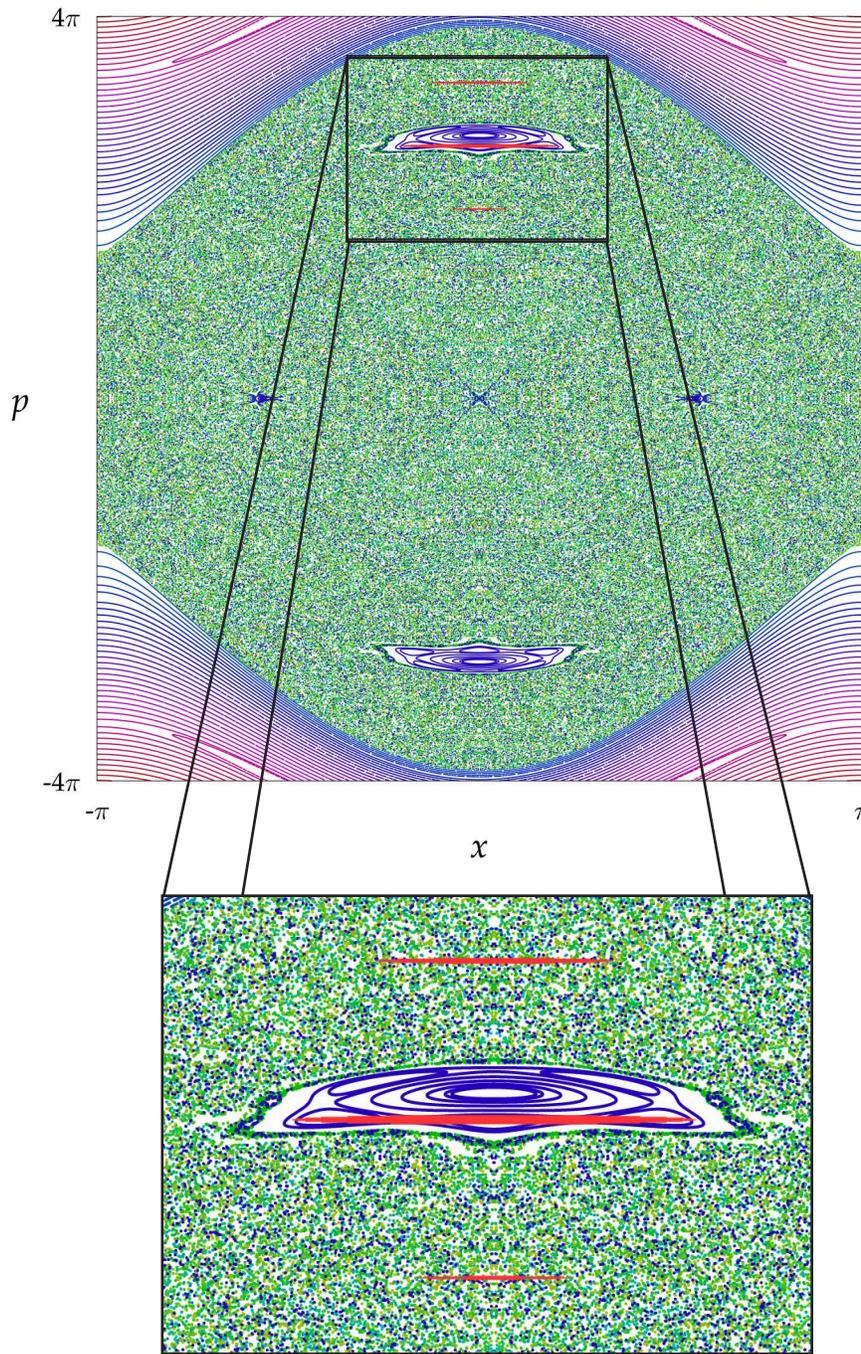
4. Free evolution of atoms in optical lattice

- nearly harmonic evolution until  $p$  is maximized



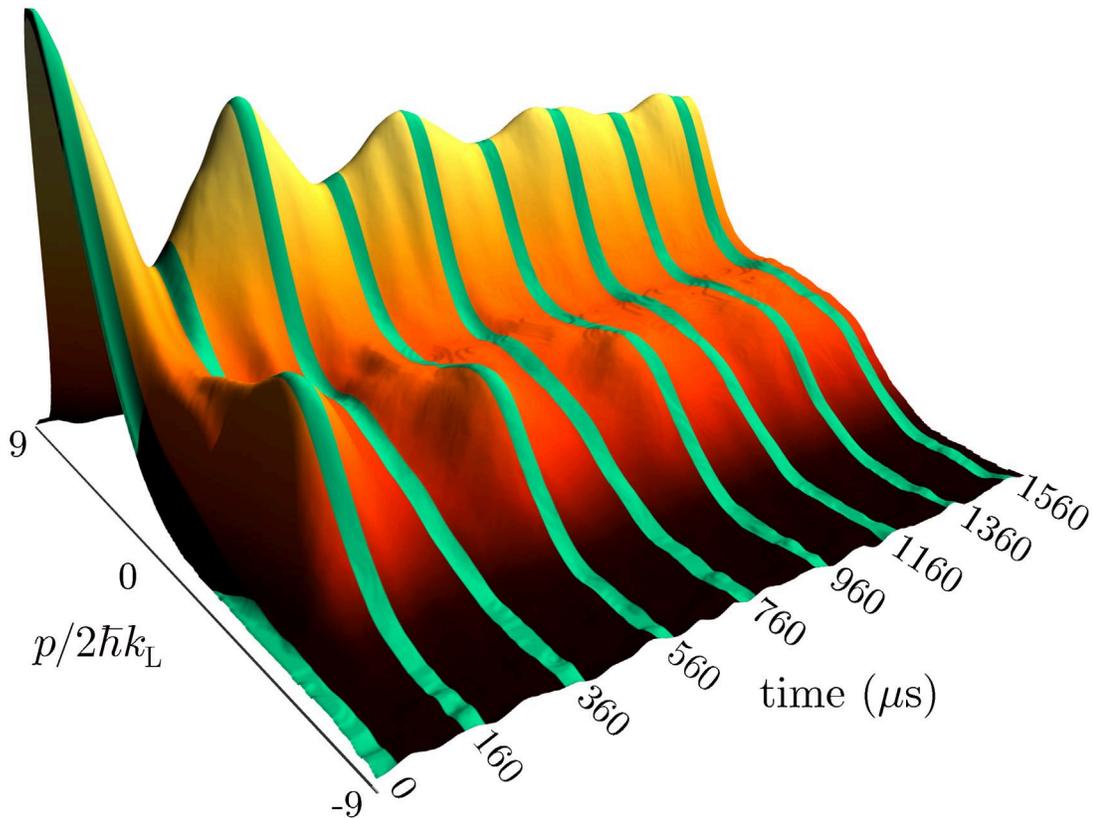
# Initial Condition in Phase Space

- Initial conditions with Raman  $\Delta p = 0.03 \times 2\hbar k_L$
- Other parameters:  $\alpha = 10.5$ ,  $\bar{k} = 2.08$

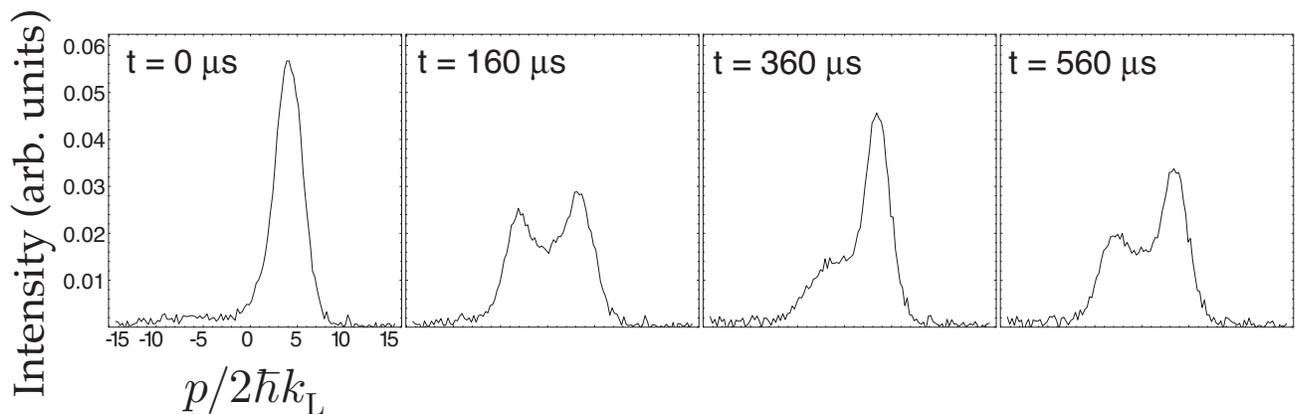


# Tunneling in Phase Space

- Experimental momentum distributions vs. time, this time with Raman  $\Delta p = 0.03 \times 2\hbar k_L$  ( $800 \mu\text{s}$  tag):

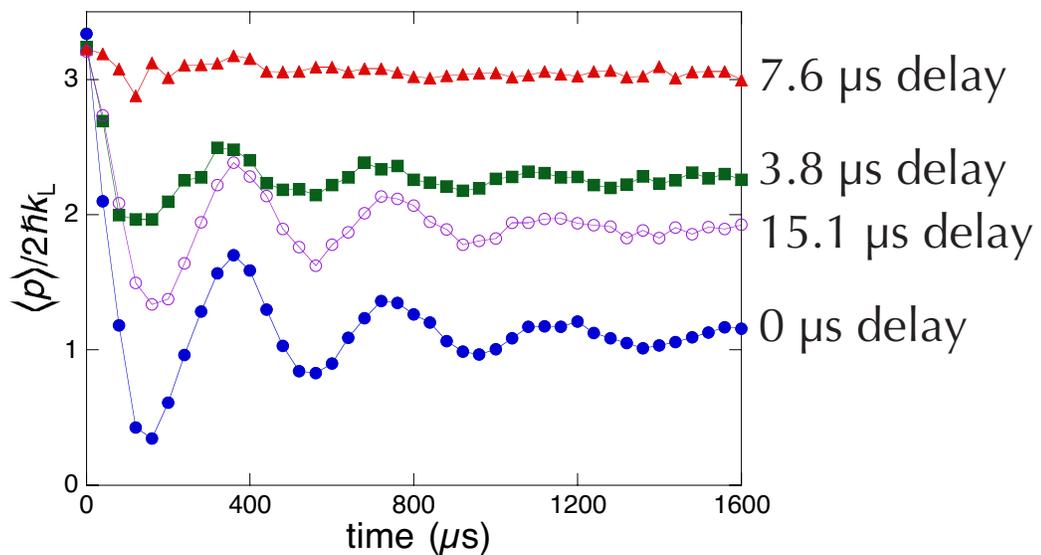
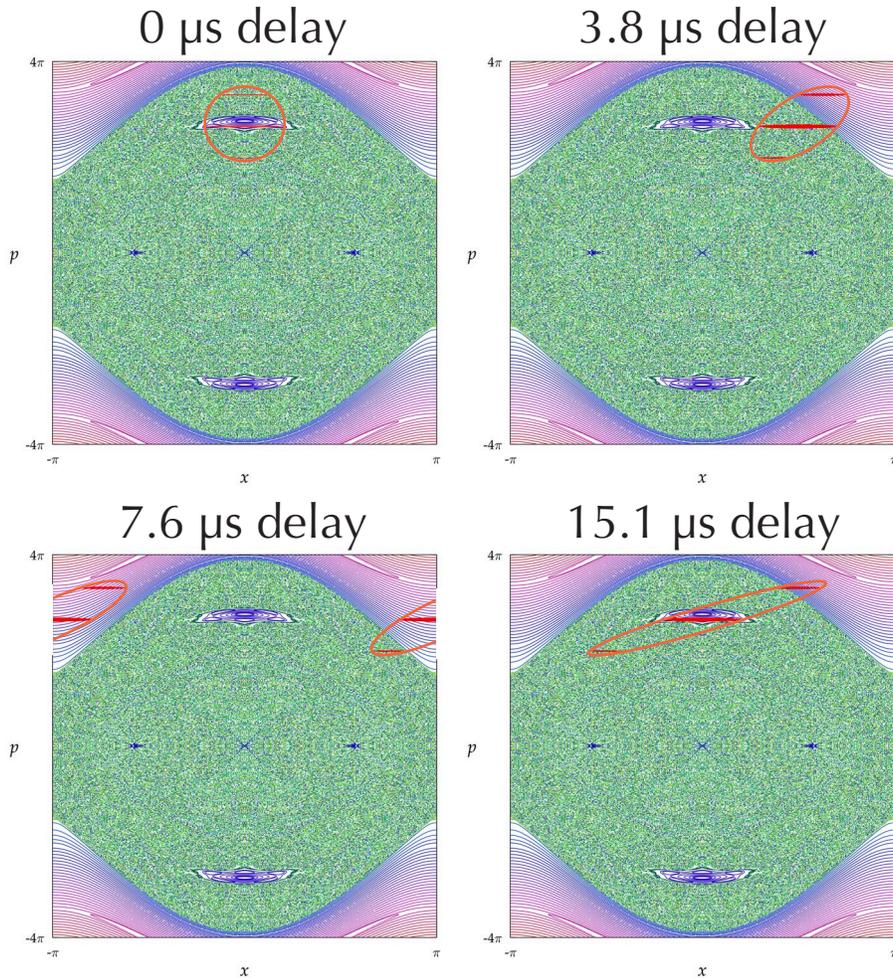


- Four oscillations before damping away
- Coherent, 16-photon transition
- Parameters:  $\alpha = 10.5$ ,  $\bar{k} = 2.08$



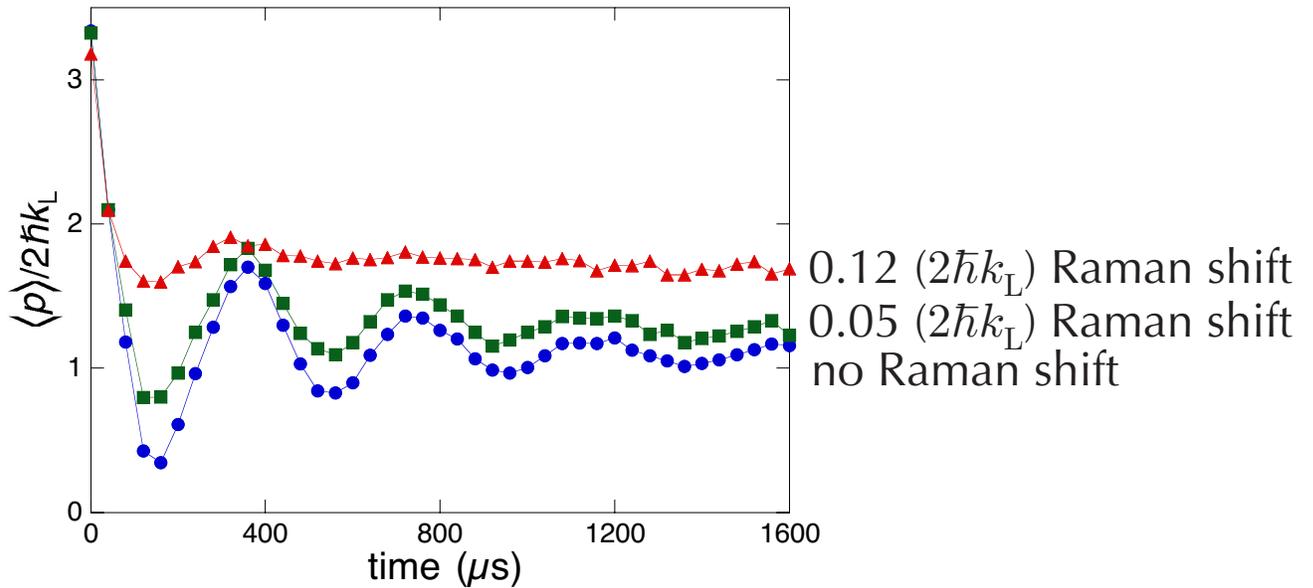
# Island Dependence

- Verify that tunneling is indeed related to classical island structure, by inserting delay time after state preparation:

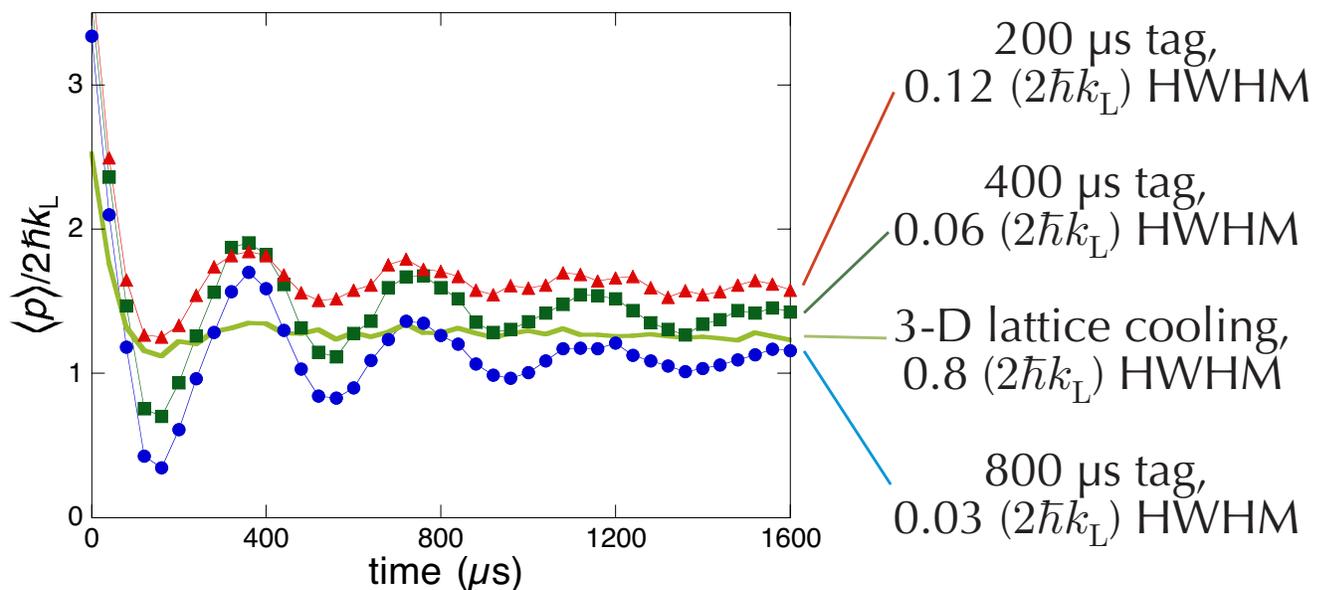


# Raman Tagging Effects

- Shift locations of velocity slices within overall shape by changing Raman detuning:



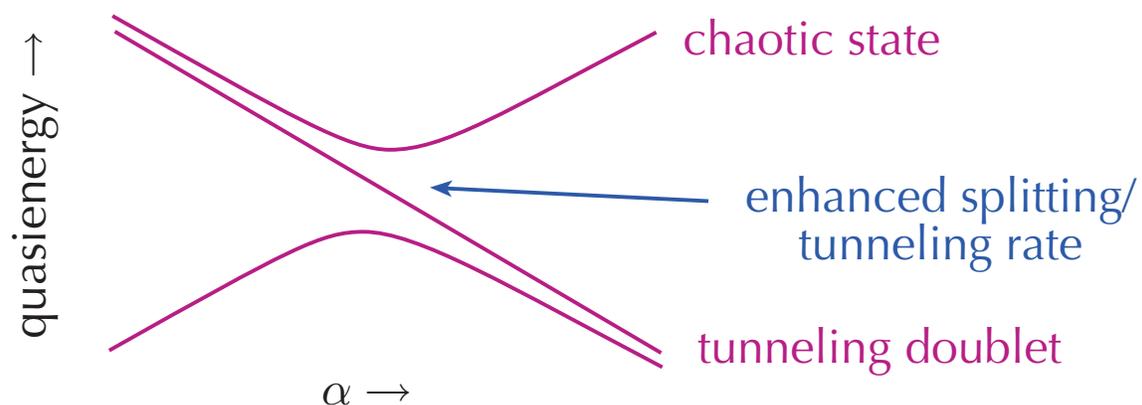
- Vary width of Raman velocity selection:



- Incomplete tunneling due mostly to Raman tag width

# Chaos-Assisted Tunneling

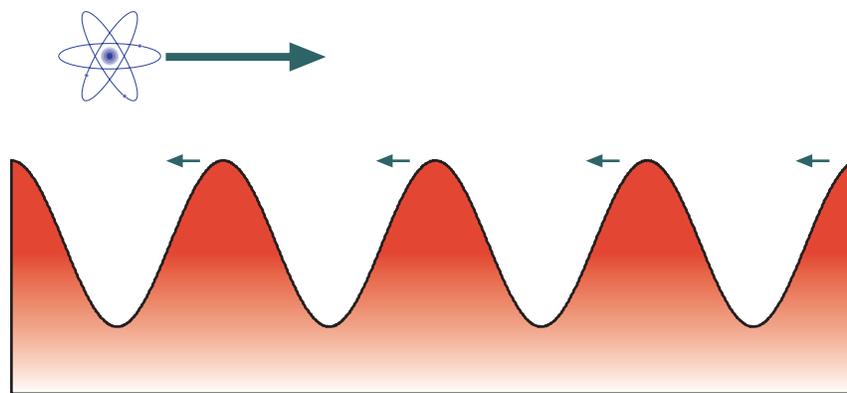
- Tunneling is “assisted” by the chaos in the sense that tunneling can be greatly enhanced by the presence of chaos
- Enhancement can be understood in two ways:
  - Quantum paths: paths through chaotic region are not attenuated as strongly as those that cross KAM tori
  - Avoided crossings: tunneling doublet can interact with a third chaotic state, prying apart the doublet



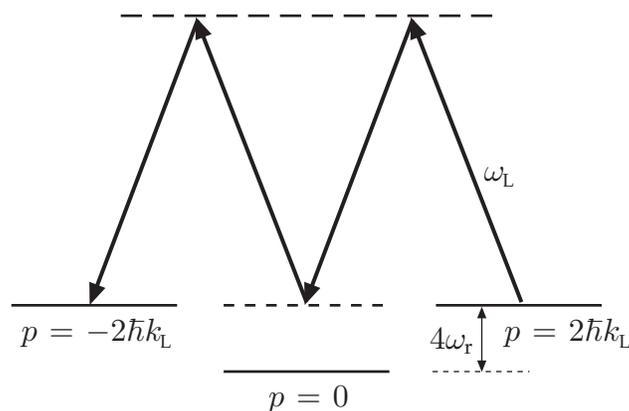
- Should be strong fluctuations in the tunneling rate as parameters vary; no universal dependence

# Bragg Scattering

- This tunneling is reminiscent of another form of tunneling in optical lattices: Bragg scattering
- Dynamical tunneling in a stationary (integrable) lattice: atom can reverse direction quantum mechanically but not classically

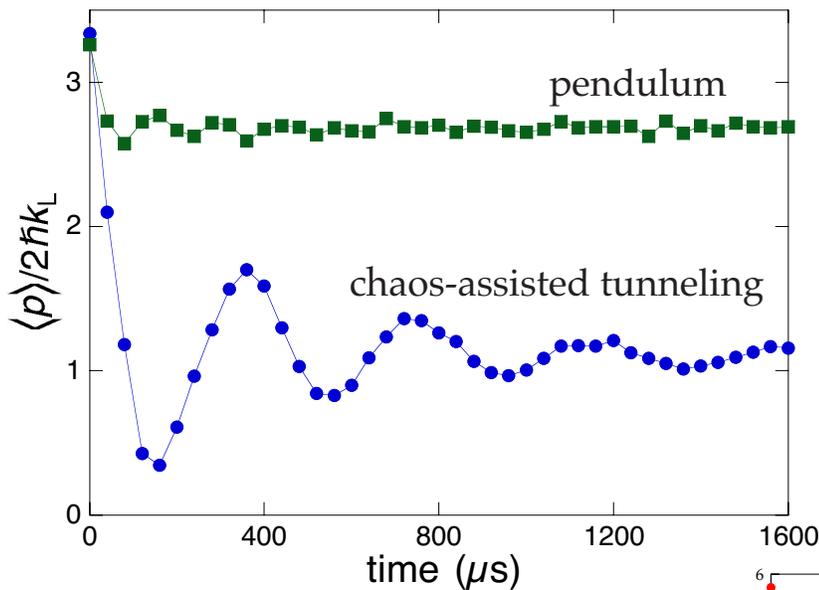
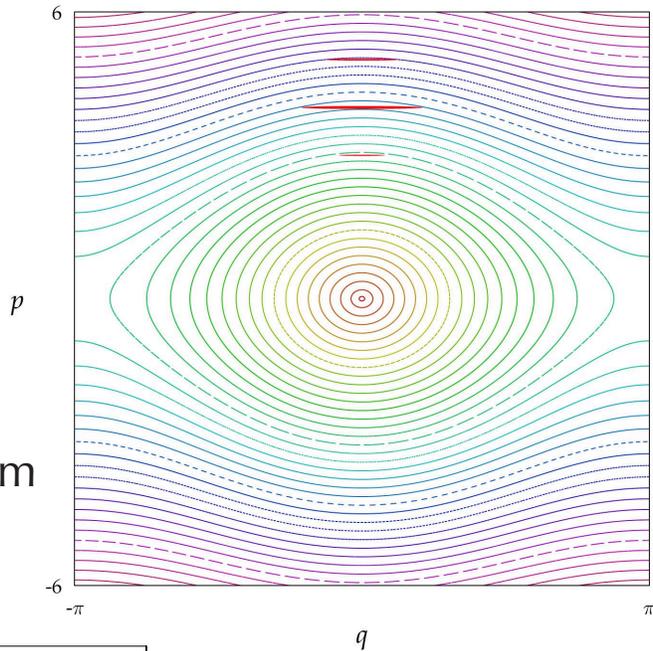


- Two-state process: transition between two symmetric plane-wave states
- Intermediate states are negligibly populated:



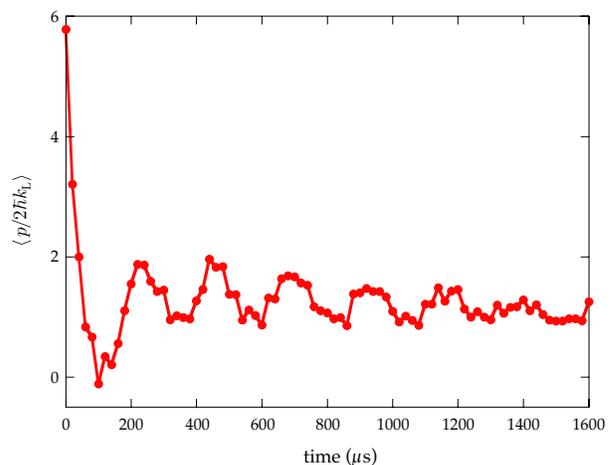
# Comparison with Integrable Tunneling

- Natural integrable counterpart of tunneling: **Bragg scattering**
- Consider time-averaged potential dynamics: **pendulum**
- Classical transport in pendulum forbidden by separatrix
- Bragg scattering provides similar transport mechanism in momentum



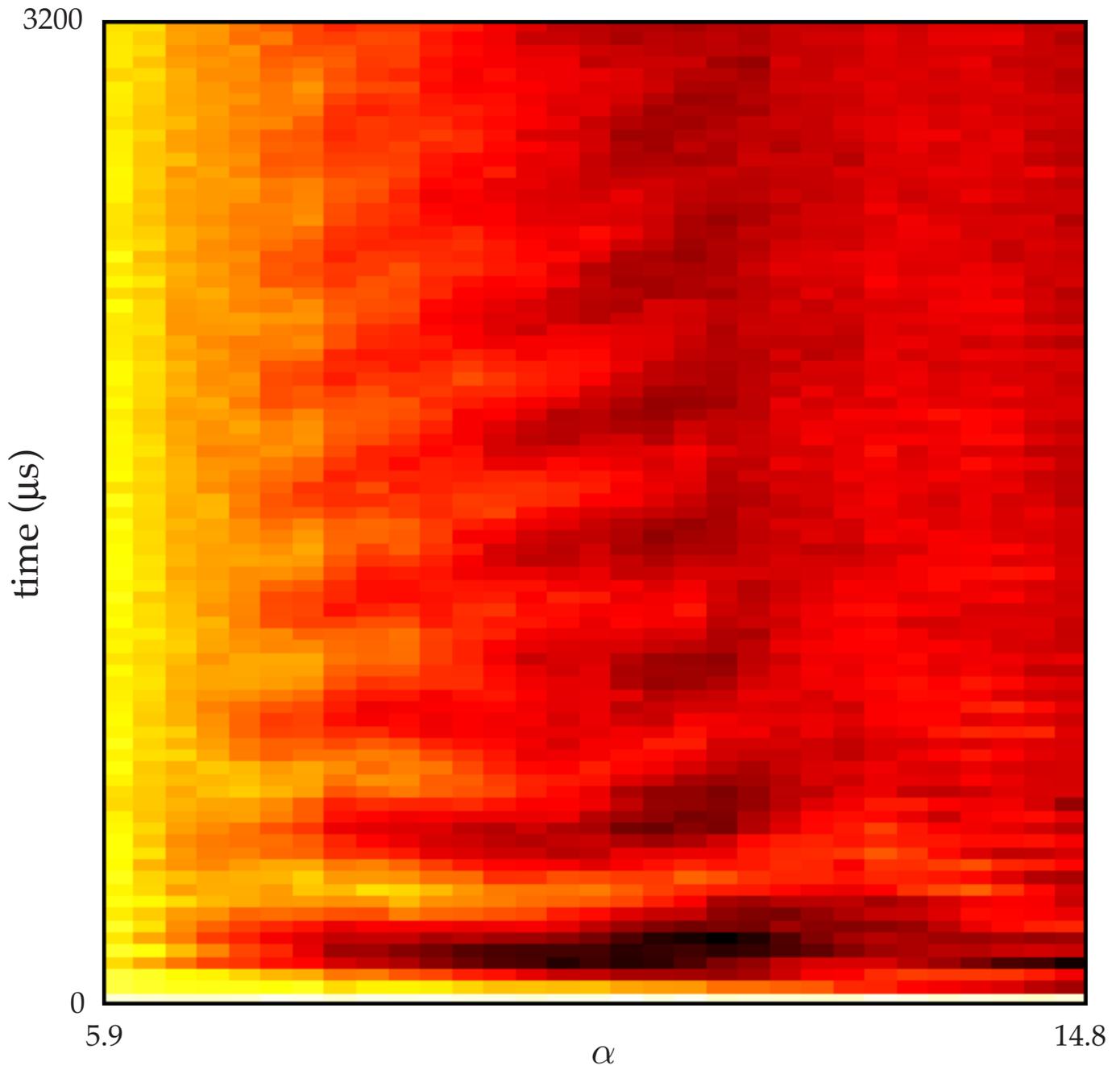
- No Bragg oscillations over time of experiment
- 8th order Bragg period for  $\alpha = 10.5$ ,  $\bar{k} = 2.1$  is 1 s

- Also 32-photon tunneling
- 16th order Bragg period for  $\alpha = 11.2$ ,  $\bar{k} = 1.0$  is 20 yr



# Tunneling Variation

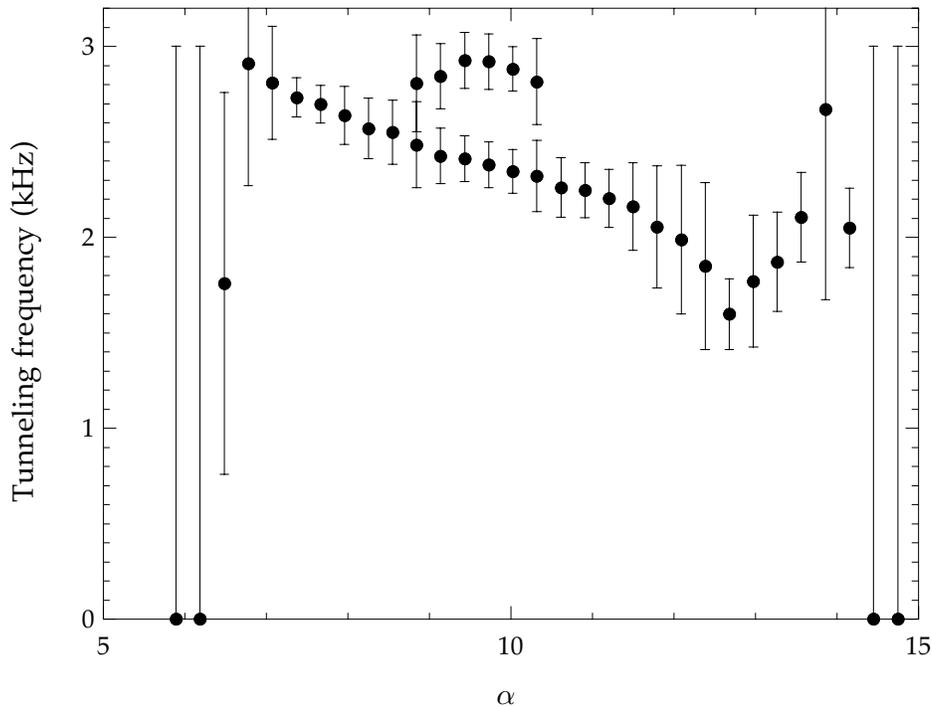
- Study dependence of tunneling on  $\alpha$  ( $\bar{k} = 2.08$ )



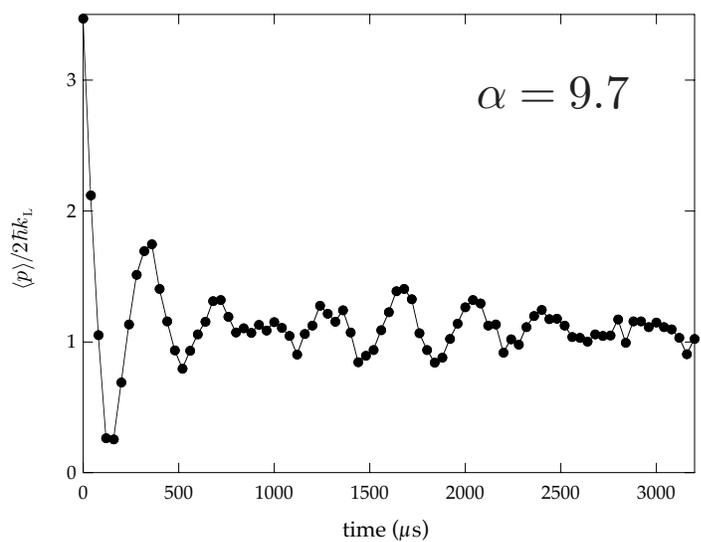
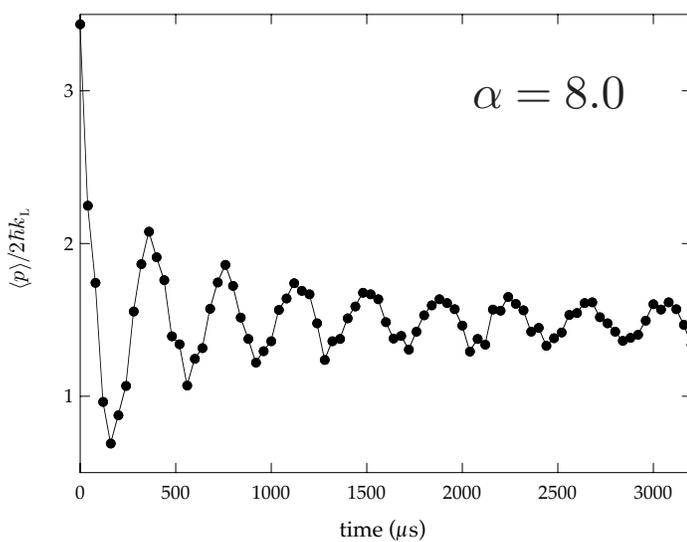
- Tunneling only visible in a relatively narrow range of  $\alpha$

# Tunneling Rate Variation

- Study dependence on tunneling rate vs.  $\alpha$  ( $\bar{k} = 2.08$ )



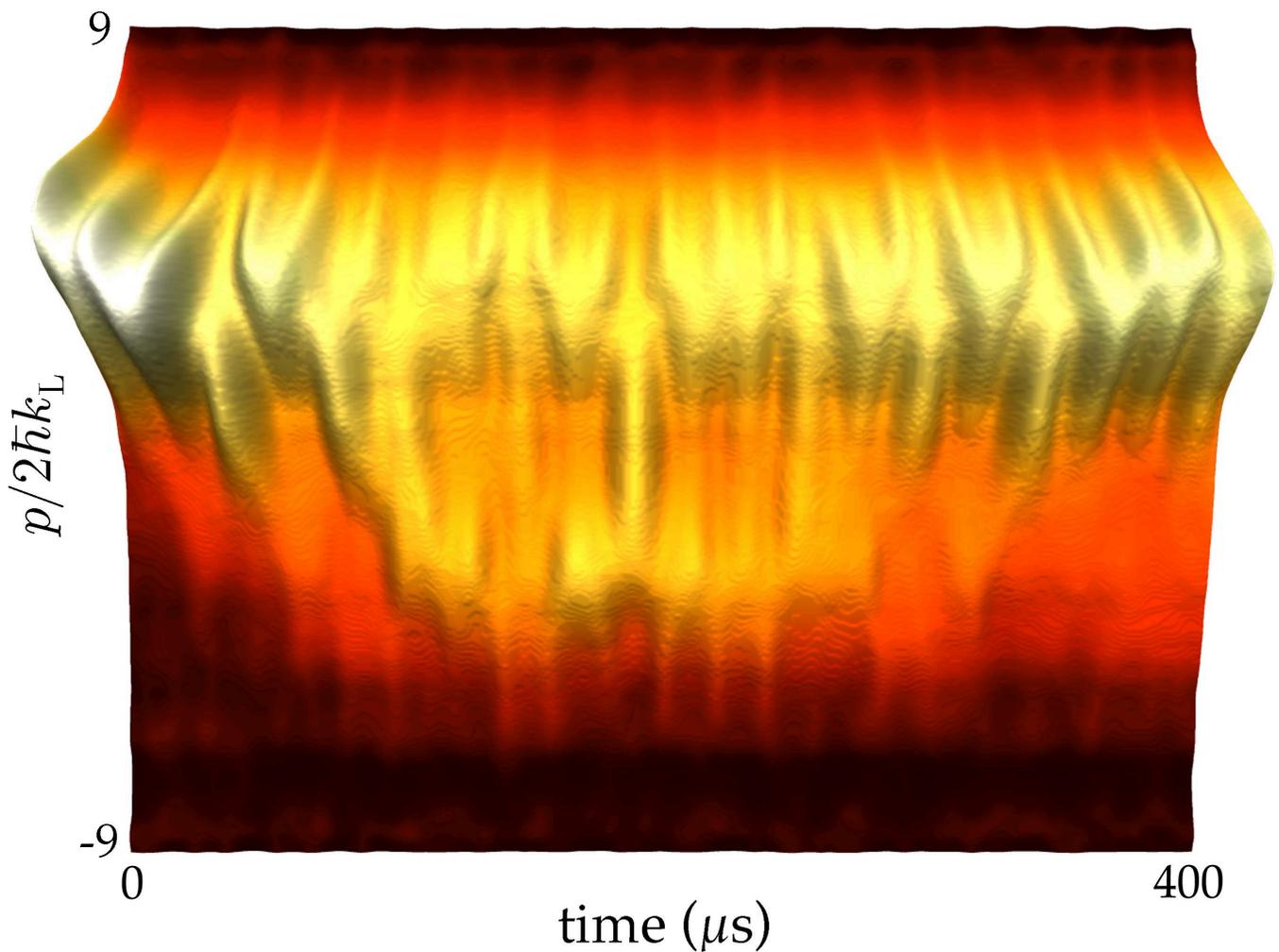
- Rate shows overall *decrease* with  $\alpha$
- Also observe both one- and two-frequency behavior



- Two-frequency behavior consistent with center of avoided crossing

# High Time Resolution

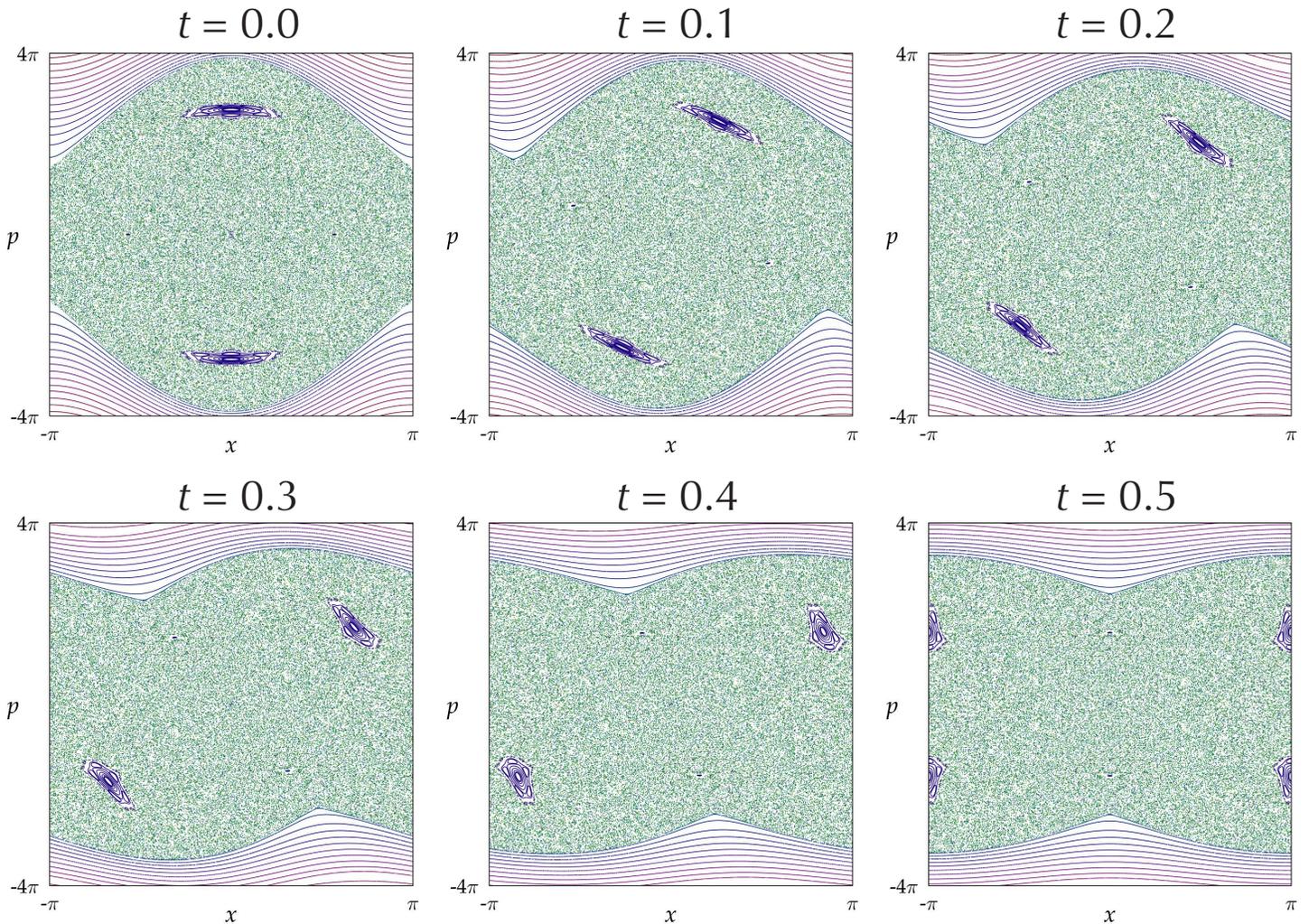
- Sample momentum distribution 10 times/modulation period
- Measurement spans 1 tunneling period,  $\alpha = 7.7$ ,  $\bar{k} = 2.08$



- Oscillations on 3 time scales:
  1. longest is tunneling
  2. shortest is classical island motion
  3. intermediate is influence of third level

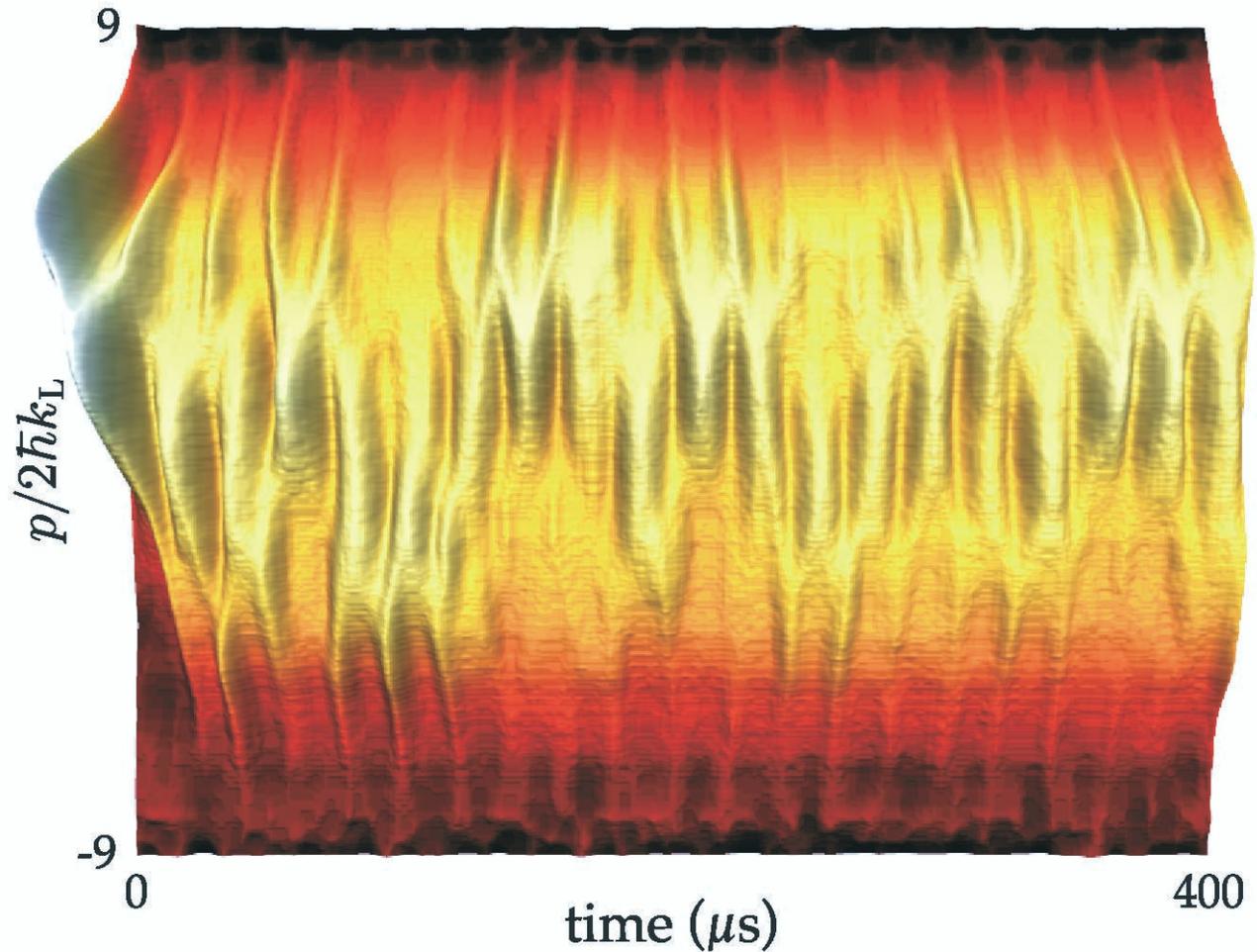
# Continuous Phase Space Evolution

- Islands move continuously between stroboscopic samples
- Islands move together during first half of modulation cycle:

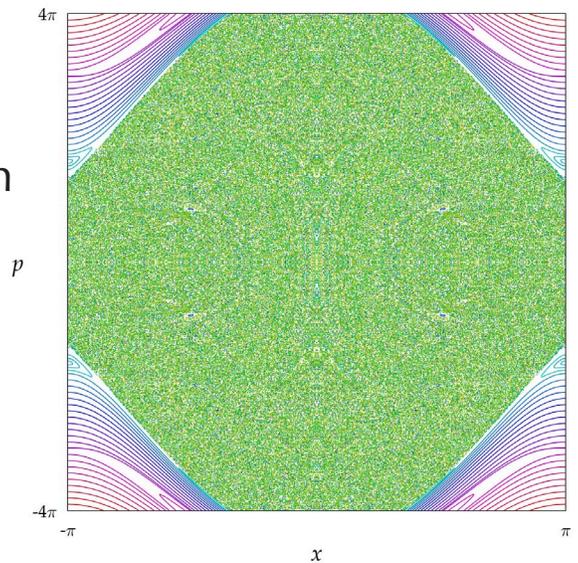


# Strongly Coupled Regime

- Measurement for  $\alpha = 17$ ,  $\bar{k} = 2.08$ :



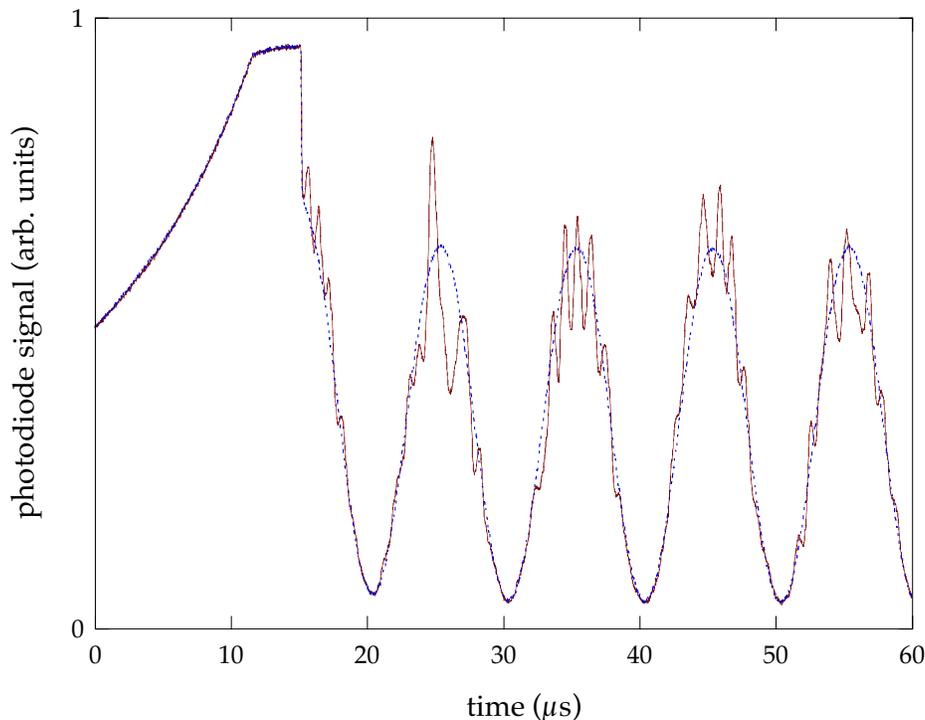
- Fast, irregular oscillations
- Classical islands have broken down
- Quantum states can no longer be grouped into doublets



# Noise and Decoherence

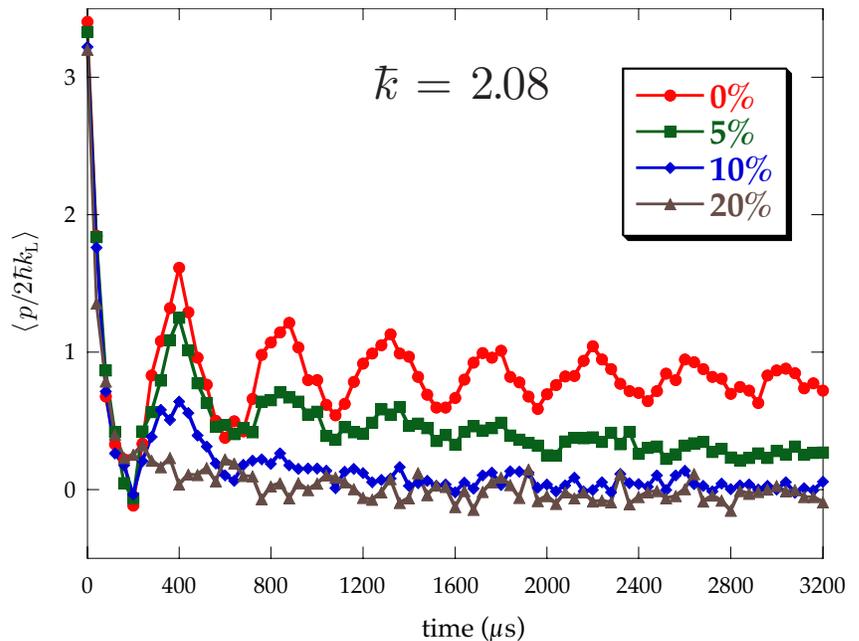
- Tunneling behavior poses problem for classical limit
  - two-state tunneling:  $\exp(-S/\hbar)$  scaling of tunneling rate ensures that macroscopic tunneling doesn't happen
  - three-state tunneling: no universal scaling of tunneling rate, so need alternate mechanism for classical behavior
- Tunneling is a coherent effect, so can be destroyed by noise or interaction with the environment (decoherence)
- Study experimentally by adding noise to the optical lattice intensity:

$$H = p^2/2 + 2\alpha[1 + \varepsilon(t)] \cos(x) \cos^2(\pi t)$$

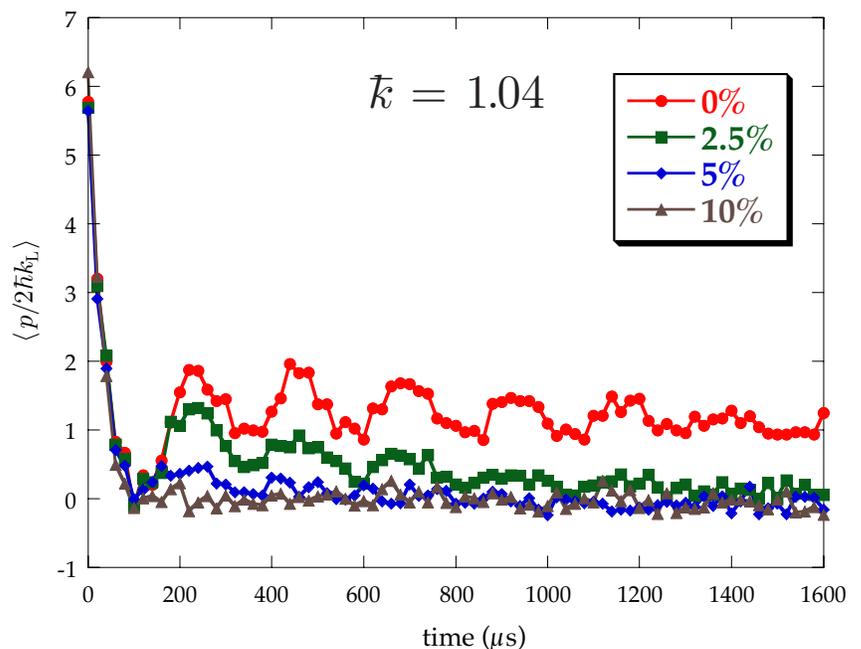


# Amplitude Noise Effects

- Can compare effects for different effective Planck constant  $\bar{k}$  ( $\alpha = 11.2$ )
- Noise level is the standard deviation compared to the average intensity
- Bandwidth-limited to the same scaled cutoff frequency for meaningful comparison



- Smaller  $\bar{k}$  is more sensitive to the noise



# Summary

- Studied chaos-assisted tunneling of cesium atoms in a modulated standing wave
- Studied several features of dynamical tunneling:
  - sensitivity to classical phase-space structure
  - sensitivity to momentum class
- Studied several features specific to CAT
  - enhancement relative to integrable tunneling
  - extra oscillation in tunneling process
  - avoided crossing behavior by varying well depth
- Noise effects
  - damping of oscillations, relaxation
  - different sensitivity for different scaled Planck constant